

Shock absorber

Formulae and examples of calculation

A shock absorber decelerates linearly. Roughly 90% of shock absorber applications can be modelled if the following 4 factors are known:

- | | | | |
|----------------------|----------|--------------------|-------------|
| 1. Mass to slow down | m (kg) | 2. Impact velocity | v_0 (m/s) |
| 3. Propelling force | F (N) | 4. Shocks per hour | C (hr) |

Symbols used in the formulae:

W_i Kinetic energy	(Nm)	M Propelling torque	(Nm)
W_p Propelling energy	(Nm)	I Moment of inertia	(kgm ²)
W_c Total energy per cycle ($W_i + W_p$)	(Nm)	g Gravity = 9,81	(m/s ²)
W_h Total energy per hour ($W_c \cdot C$)	(Nm/hr)	h Drop height exc. shock abs. stroke	(m)
me Effective weight	(kgme)	s Shock absorber stroke	(m)
m Mass to slow down	(kg)	Q Reactive force	(N)
$*v$ Velocity or moving mass	(m/s)	μ Friction coefficient	
$*v_0$ Impact velocity of shock absorber	(m/s)	t Braking time	(sec)
ω Angular velocity	(rad/s)	a Deceleration	(m/sec ²)
F Propelling force	(N)	α Side load angle	(°)
C Number of Shocks per hour	(/hr)	β Angle of inclination	(°)
P Motor power	(kW)	L Radius of mass	(m)
ST Setting coefficient (normally 2.5)	1 to 2.5	R Dist. pivot/installation pt. of damp.	(m)
		r Dist. pivot/force application pt.	(m)

* v or v_0 is the impact velocity of the mass. In the case of an accelerated movement (for example when the mass is displaced by a pneumatic cylinder), the impact velocity can be 1.5 to 2 times greater than the average velocity.

1. Mass without propelling force

Formulae:

$$W_i = m \cdot v^2 \cdot 0,5$$

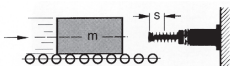
$$W_p = 0$$

$$W_c = W_i + W_p$$

$$W_h = W_c \cdot C$$

$$v_0 = v$$

$$me = m$$



2. Mass with propelling force

Formulae:

$$W_i = m \cdot v^2 \cdot 0,5$$

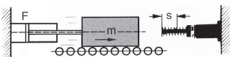
$$W_p = F \cdot s$$

$$W_c = W_i + W_p$$

$$W_h = W_c \cdot C$$

$$v_0 = v$$

$$me = \frac{2 \cdot W_c}{v_0^2}$$



2.1 Mass moving upwards

$$W_c = (F + m \cdot g) \cdot s$$

2.2 Mass moving downwards

$$W_c = (F + m \cdot g) \cdot s$$

3. Mass pulled by a motor

Formulae:

$$W_i = m \cdot v^2 \cdot 0,5$$

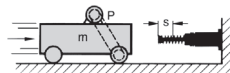
$$W_p = \frac{1000 \cdot P \cdot ST \cdot s}{V}$$

$$W_c = W_i + W_p$$

$$W_h = W_c \cdot C$$

$$v_0 = v$$

$$me = \frac{2 \cdot W_c}{v_0^2}$$



4. Mass on motorised rollers

Formulae:

$$W_i = m \cdot v^2 \cdot 0,5$$

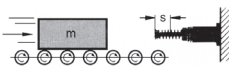
$$W_p = m \cdot \mu \cdot g \cdot s$$

$$W_c = W_i + W_p$$

$$W_h = W_c \cdot C$$

$$v_0 = v$$

$$me = \frac{2 \cdot W_c}{v_0^2}$$



5. Swinging mass with propelling force

Formulae:

$$W_i = m \cdot v^2 \cdot 0,5$$

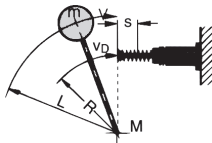
$$W_p = \frac{M \cdot s}{R}$$

$$W_c = W_i + W_p$$

$$W_h = W_c \cdot C$$

$$v_0 = \frac{L}{R} \cdot \omega \cdot R$$

$$me = \frac{2 \cdot W_c}{v_0^2}$$



Formulae and examples of calculation

6. Free falling mass

Formulae:

$$W^1 = m \cdot g \cdot h$$

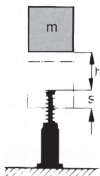
$$W^2 = m \cdot g \cdot s$$

$$W^3 = W^1 + W^2$$

$$W^4 = W^3 \cdot C$$

$$v^0 = \sqrt{2 \cdot g \cdot h}$$

$$me = \frac{2 \cdot W^3}{v^0^2}$$



6.1 Mass rolling or sliding on an inclined plane

Formulae:

$$W^1 = m \cdot g \cdot h = m \cdot v^0^2 \cdot 0,5$$

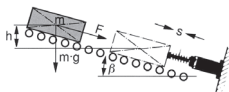
$$W^2 = m \cdot g \cdot \sin\beta \cdot s$$

$$W^3 = W^1 + W^2$$

$$W^4 = W^3 \cdot C$$

$$v^0 = \sqrt{2 \cdot g \cdot h}$$

$$me = \frac{2 \cdot W^3}{v^0^2}$$



6.1a Mass with upwards propelling force

$$W^2 = (F - m \cdot g \cdot \sin\beta) \cdot s$$

6.1b Mass with downwards propelling force

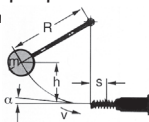
$$W^2 = (F + m \cdot g \cdot \sin\beta) \cdot s$$

6.2 Mass free falling about a pivot point

Formulae: Follow calculation

for example 6.1. Verify the radial load.

$$\tan \alpha = \frac{s}{R}$$



7. Rotary index table with propelling torque

Formulae:

$$W^1 = m \cdot v^2 \cdot 0,25$$

$$W^2 = \frac{M \cdot s}{R}$$

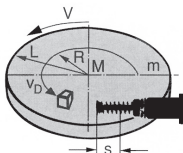
$$W^3 = W^1 + W^2$$

$$W^4 = W^3 \cdot C$$

$$v^0 = \frac{v \cdot R}{L} = \omega \cdot R$$

$$me = \frac{2 \cdot W^3}{v^0^2}$$

NOTE: mass evenly spread.



8. Rotating mass with propelling torque

Formulae:

$$W^1 = m \cdot v^2 \cdot 0,18$$

$$W^2 = \frac{M \cdot s}{R}$$

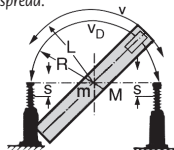
$$W^3 = W^1 + W^2$$

$$W^4 = W^3 \cdot C$$

$$v^0 = \frac{v \cdot R}{L} = \omega \cdot R$$

$$me = \frac{2 \cdot W^3}{v^0^2}$$

NOTE: mass evenly spread.



9. Rotating mass with propelling force

Formulae:

$$W^1 = m \cdot v^2 \cdot 0,18$$

$$W^2 = \frac{F \cdot r \cdot s}{R} = \frac{M \cdot s}{R}$$

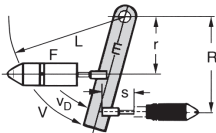
$$W^3 = W^1 + W^2$$

$$W^4 = W^3 \cdot C$$

$$v^0 = \frac{v \cdot R}{L} = \omega \cdot R$$

$$me = \frac{2 \cdot W^3}{v^0^2}$$

NOTE: mass evenly spread.



10. Mass in controlled descent without propelling force

Formulae:

$$W^1 = m \cdot v^2 \cdot 0,5$$

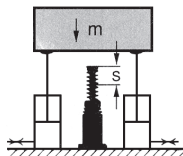
$$W^2 = m \cdot g \cdot s$$

$$W^3 = W^1 + W^2$$

$$W^4 = W^3 \cdot C$$

$$v^0 = v$$

$$me = \frac{2 \cdot W^3}{v^0^2}$$



Reactive force Q(N)

$$Q = \frac{1,2 \cdot W^3}{s}$$

Braking time (s)

$$t = \frac{2,6 \cdot s}{v^0}$$

Deceleration (m/s²)

$$a = \frac{0,6 \cdot v^0^2}{s}$$

These formulae will give you approximate values to assist in the selection of a shock absorber but a safety margin should always be applied. (Precise values can only be calculated if actual parameters are known).